

# 4.4 Complex Numbers

Name:

Date:

**Vocabulary**

imaginary unit

pure imaginary number

complex number

complex conjugate

**SAT WARNING:** A store charges \$49 for a pair of pants. This price is 40% more than the amount it costs the store to buy the pants. After a sale, any employee is allowed to purchase any remaining pairs of pants at 30% off the store's cost. How much would it cost an employee to purchase the pants after the sale?

*separate  
separate*

*so  $i = \sqrt{-1}$*

1. The imaginary unit  $i$  is defined to be  $i^2 = -1$ .

pure imaginary numbers are  $2i, -6i, i\sqrt{3}$  (square roots of neg real #s)

**IMPORTANT:**  $\sqrt{-b} = i\sqrt{b}$  *Key Concept - pull -1 out*

- a.  $\sqrt{-25}$  *5i*
- b.  $\sqrt{-28}$  *2i $\sqrt{7}$*
- c.  $\sqrt{-32}$   *$\sqrt{16}\sqrt{2}\sqrt{-1}$   
 $4i\sqrt{2}$*
- d.  $\sqrt{-125}$   *$\sqrt{25}\sqrt{5}\sqrt{-1}$   
 $5i\sqrt{5}$*



2.  $i^1 = i, i^2 = -1, i^3 = -i, i^4 = 1$  (Show Circle)

*MISS* Divide by 4 Remainder

$i^0 = 1$   
 $i^1 = i$   
 $i^2 = -1$   
 $i^3 = -i$   
 $i^4 = 1$

$i^{28} = 3$   
 $i^{-1}$

What is  $i^{31}$ ?

**3. Products of Pure Imaginary Numbers**

- a.  $-3i \cdot 2i$   
 *$-6(i^2)$   
 $-6(-1)$   
 $6$*
- b.  $\sqrt{-12} \cdot \sqrt{-2}$   
 *$\sqrt{24}$   
 $4\sqrt{6}$   
 $2i\sqrt{3} \cdot 2i$   
 $-4i^2$   
 $-4(-1)$   
 $4$*

**4. Equations with Pure Imaginary Solutions**

- a.  $x^2 + 64 = 0$   
 *$x^2 = -64$   
 $x = \pm\sqrt{-64}$   
 $x = \pm 8i$*
- b.  $5y^2 + 20 = 0$   
 *$5(y^2 + 4) = 0$   
 $y^2 + 4 = 0$   
 $y = \pm\sqrt{-4}$   
 $\pm 2i$*

**5. Complex Numbers:  $2+3i$**  a real number and a pure imaginary number can't combine - just stay that way

- a. Add/Subtract: add/subt real parts, and add/subt imaginary parts
  - i.  $(3+5i)+(2-4i)$   *$5+i$*
  - ii.  $(4-6i)-(3-7i)$   *$-1+i$   
 $4-3$*

**b. Equate: What make the equation true?**

$2x+yi=-14-3i$

$2x+yi=14$   
 $yi=-3i$   
 $x=7$   
 $y=-3$   
 $5x+1+(3+2y)i=4$   
 $2x-2+(y+6)i$   
 $5x+1=2x-2 \Rightarrow 3x=-3 \Rightarrow x=-1$

*$(3+2y)i = (4-6i) - (4-6i) - 3i + 2i = -1-i$   
 $-3i + 2i = -1-i$   
 $-i = -1$   
 $i = 1$*

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7. In Class Practice # 1-17

8. Honors Group Work

1. Jennifer and Jessica come up with different answers to the same problem. They had to multiply  $(4 + i)(4 - i)$  and give their answer as a complex number. Jennifer claims that the answer is 15 and Jessica claims that the answer is 17. Who is correct? Explain.

2. Always, sometimes, never? Every complex number has both a real part and an imaginary part. Explain

3. Simplify  $(1 + 2i)^3$



Practice at Home: 4.4 #18-58 Even (These are simple - just need practice)

5c. Multiplying Complex numbers - USE FOIL

Electricity: In an AC circuit, the voltage  $E$ , current  $I$ , and impedance  $Z$ , are related by the formula  $E = I \cdot Z$ . Find the voltage in a circuit with current  $1+4j$  amps and impedance  $3-6j$  ohms.

$$\begin{aligned} & (1+4j)(3-6j) \\ & 3 + 6j - 24j^2 \\ & \quad - 24(-1) \\ & 3 + 6j + 24 \\ & \quad (27+6j) \end{aligned}$$

6. Dividing Complex numbers, (simplifying) - use the COMPLEX CONJUGATE  
(imaginary number in denominator is not simplified!)

Conjugate of  $3+4j$  is  $3-4j$

a. Simplify  $\frac{5i}{3+2i}$

$$\begin{aligned} & \frac{5i(3-2i)}{(3+2i)(3-2i)} \\ & \frac{15i - 10i^2}{13} \end{aligned}$$

$$\frac{9 - 4i^2}{13 + 10i}$$

$$\sqrt{\frac{10}{13} + \frac{5}{13}i}$$

b. Simplify  $\frac{5+i}{2i}$

$$\frac{(5+i)(-2i)}{2i(-2i)}$$

$$\frac{10i - 2}{-4}$$

$$\frac{-11}{2 - 2i}$$

$$\frac{1}{2} \frac{5i}{1 - i}$$